



**2024 ENGINEERING INSTITUTION OF ZAMBIA  
SYMPOSIUM**

**DECISION MAKING FOR AN OPTIMIZED COBALT AND  
COPPER DISSOLUTION AS ASSISTED BY THE  
MULTI-CRITERIA ANALYSIS**

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Zambia**

# Co-Cu ore dissolution optimized by means of MCDA

## Outline of the presentation

**Context of the study**

**Motivation of the study**

**Aim and objectives**

**Background**

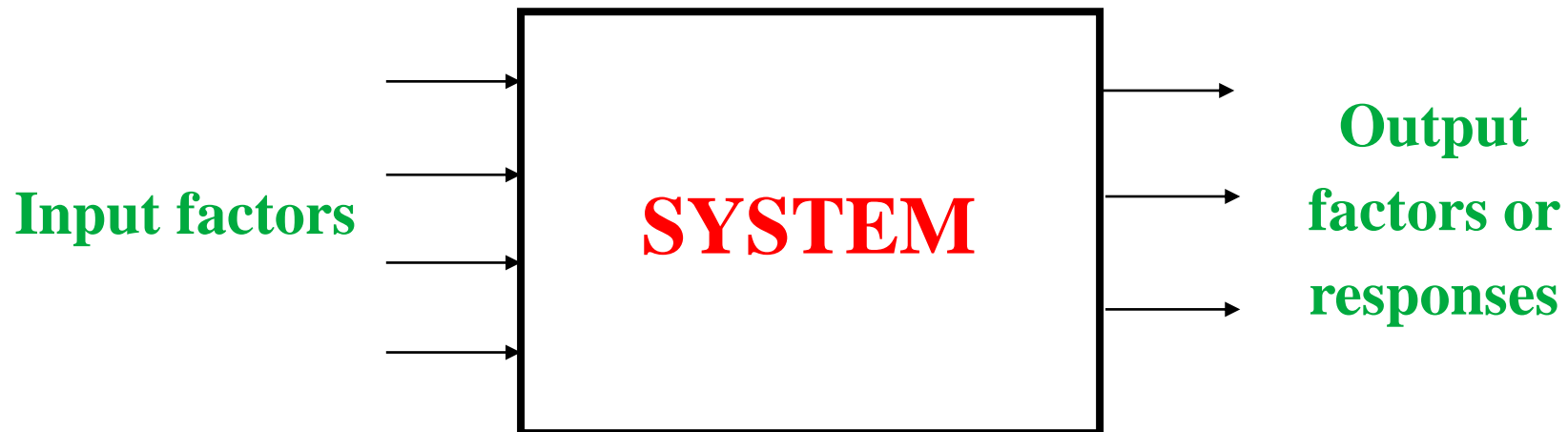
**Methodology**

**Findings and discussions**

**Conclusion**

# Co-Cu ore dissolution optimized by means of MCDA

- Context of the study
- The **system** being studied is the **leaching** (dissolution) of Cu-Co ore
- The **leaching system** is modeled as a **MIMO** (multiple-input and multiple-output)



# Co-Cu ore dissolution optimized by means of MCDA

- Context of the study (cont'd 1)
- In this system (**leaching of ore**),

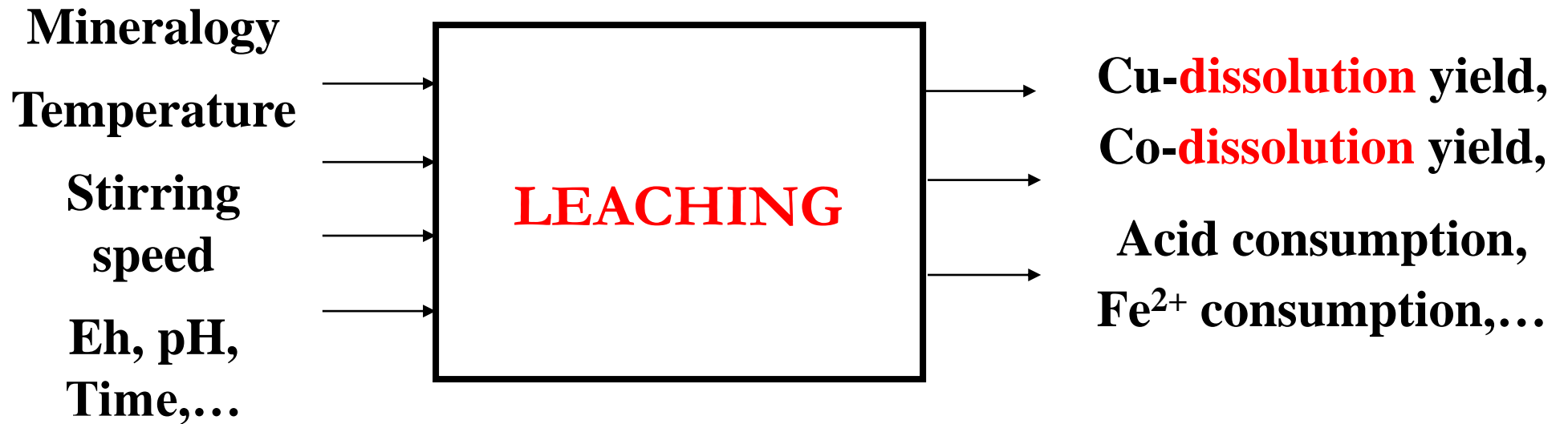
Some input **parameters** may exhibit **interactions**

Some output parameters or **responses** may be **correlated**

Certain input and output **variables** may have **dependencies** or **independences**

# Co-Cu ore dissolution optimized by means of MCDA

- Context of the study (cont'd 2)
- Schematically



# Co-Cu ore dissolution optimized by means of MCDA

- **Motivation of the study**
- To **improve** the **dissolution** of Cu-Co ore, MCDA is employed

MCDA allows us to select one or more optimal solutions, **in the Pareto** sense, from a discrete set of possible solutions.

MCDA is used for the following reasons:

- ✓ It enables the representation and **hierarchical decomposition** of **complex** problems into **separate elements**.
- ✓ It logically **groups** and **classifies** elements according to coherent and logical criteria.

# Co-Cu ore dissolution optimized by means of MCDA

- **Aim and objectives**
- The **purpose** of this study is to **optimize** and **analyze** the factors that influence the **recovery** of Cu and Co.
- The specific **objectives** of the study are as follows:
  - ✓ To examine the **relationship** between input and output variables.

# Co-Cu ore dissolution optimized by means of MCDA

- **Aim and objectives (cont'd)**
- **The specific objectives of the study are as follows:**
  - ✓ To assess the **influence** of each input parameter on the dissolution of Cu and Co
  - ✓ To establish the **criteria** for optimizing the recovery of Cu and Co.
  - ✓ To determine the **optimal conditions** for the dissolution of Cu and Co from a complex ore.



# Co-Cu ore dissolution optimized by means of MCDA

- **Background**

- **Tapia et al., (2023)** have drawn up a table showing how **uncertainty** is assessed in sustainable system planning using multi-criteria decision analysis methods
- **Mbuya and Mulaba (2023)** suggested **MCDM** (multicriteria decision making) methods by showing the importance of using these methods to study a **leaching system**, with multiple inputs and multiple outputs (**MIMO**), **optimized** by the response surface methodology (RSM) and artificial neural networks (ANN).

# Co-Cu ore dissolution optimized by means of MCDA

## • Background (cont'd 1)

- Baloyi and Meyer (2020) evaluated multi-criteria decision methods in detail to **develop a mining method selection model**.
- Among multicriteria decision methods, the **Analytical hierarchy process (AHP)** method is **well known**, very **popular**, widely used and **documented** (Gass and Rapcsak, 2004; Mardini et al., 2015; Perzina and Ramik, 2014; Patia et al., 2023).
- Several works that have used **AHP** have been reported in the literature (Rauscher, 2003; Kostagiolas, 2012; Abdullah et al., 2013; Saranya et al., 2021).

# Co-Cu ore dissolution optimized by means of MCDA

- **Background (cont'd 2)**

- **AHP** was developed by Saaty and then extensively studied and refined (Saaty and Peniwati, 2008; Saaty, 2008).
- The AHP method integrates **various criteria** to arrive at a justified choice of technology. When the decision is made using this method, it is considered to be **rational, systematic, and correct**.
- It provides a complete and rational framework for **structuring** decision-making, representing, and evaluating elements, **in order to link them to objectives and evaluate alternative solutions** (Roy, 2005).

# Co-Cu ore dissolution optimized by means of MCDA

## • Methodology

- The **laboratory conducted leaching tests** by combining varying quantities of crushed ores, which passed through a 75  $\mu\text{m}$  sieve, with sulfuric acid (98%  $\text{H}_2\text{SO}_4$ ) in a 1000 mL beaker.
- These tests followed the **Taguchi  $L_{25}$  experimental design ( $5^5$ )**.
- The parameters investigated included **time** (2, 2.5, 3, 3.5, and 4 h), **percentage of solid** (20, 25, 30, 35, and 40%), **stirring speed** (500, 600, 700, 800, and 900 rpm), **sulfuric acid concentration** (40, 50, 60, 70, and 80 g/L), and  **$\text{Fe}^{2+}$  ion concentration** (2, 3, 4, 5, and 6 g/L). **Mechanical agitation** was used, and the **temperature** was maintained at **60 °C**.

# Co-Cu ore dissolution optimized by means of MCDA

- **Methodology (cont'd 1)**
- **Multi-criteria decision analysis is used in conjunction with the Taguchi approach to optimize the leaching process of Cu-Co ore. Among the various MCDA methods, the Analytic Hierarchy Process (AHP) is the one utilized in this study.**
- **The 5 steps of AHP are: (1) Establish the hierarchical structure, (2) Perform binary weightings, (3) Determine the eigenvectors, (4) Calculate the consistency ratio (CR) and, (5) Establish final priorities**

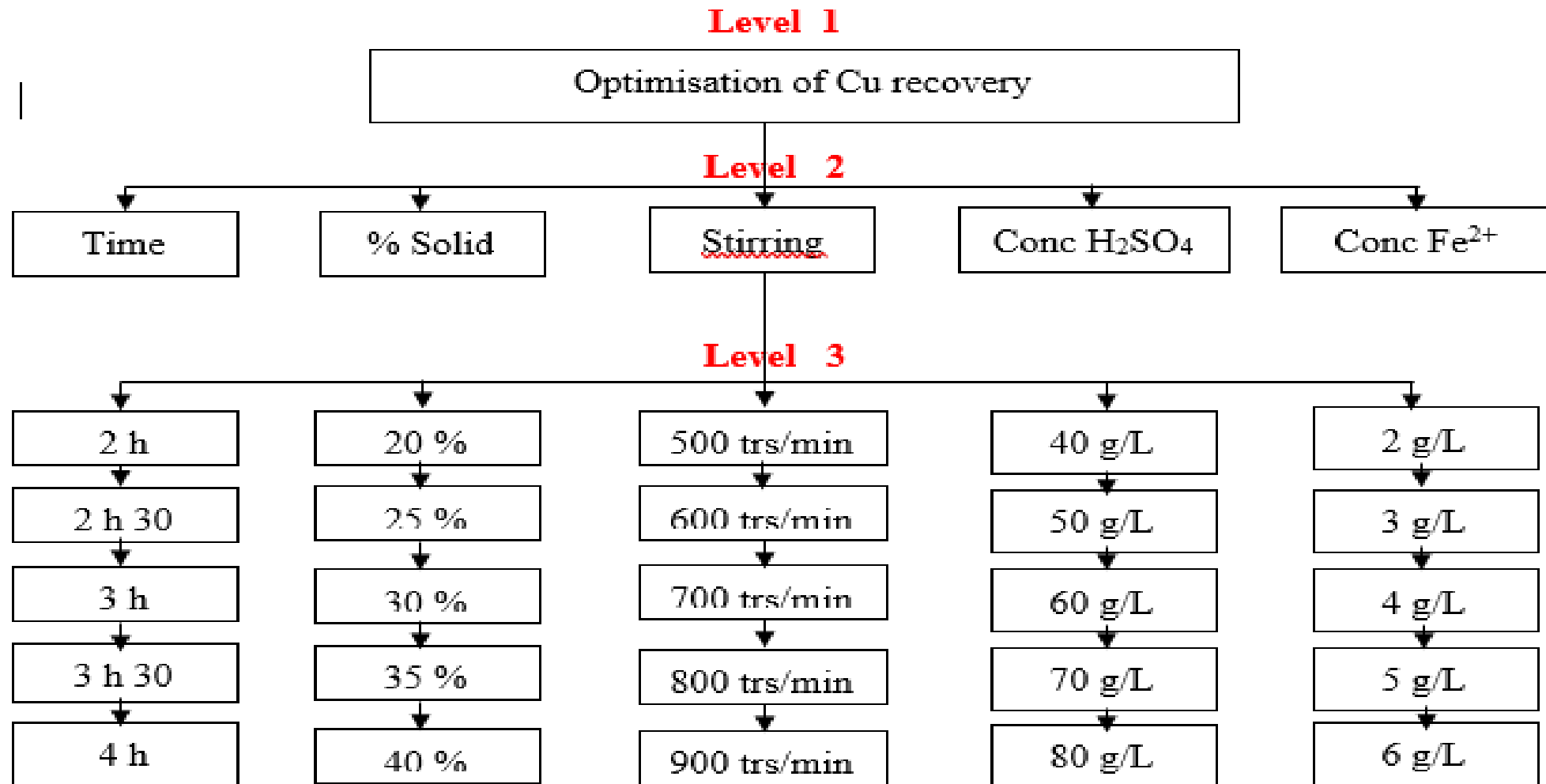
# Co-Cu ore dissolution optimized by means of MCDA

- **Methodology (cont'd 2)**

- **Three hierarchical levels have been established. Level 1 focuses on the objective, which is the optimization of Cu dissolution. Level 2 examines the parameters under study, namely time, solid percentage, agitation, acidity, and ferrous ion concentration, and compares them to the objective.**
- **Lastly, Level 3 delves into the specific terms of each parameter. For instance, in the case of acidity, the values considered are 40, 50, 60, 70, and 80 g/L.**

# Co-Cu ore dissolution optimized by means of MCDA

- Methodology (cont'd 3)



# Co-Cu ore dissolution optimized by means of MCDA

- **Methodology (cont'd 4)**
- **Pairwise comparisons** are carried out for the second and third level of the hierarchy following the Saaty comparison scale. They are carried out based on the **signal/noise** ratios previously obtained with the Taguchi method.
- For each comparison, we chose the **most important criterion** and expressed the **judgment as to its importance**.



# Co-Cu ore dissolution optimized by means of MCDA

- Findings and discussions

- The chemical and mineralogical **composition** of the composite ore sample are shown in Table 1

**Table 1: Chemical and Mineralogical composition of the composite ore**

Elements	Cu	Co	Fe	Zn	Mn	Pb	SiO <sub>2</sub>	CaO	MgO
Percentage (%)	3.49	0.20	4.21	0.07	0.91	0.01	57.03	4.74	5.84

# Co-Cu ore dissolution optimized by means of MCDA

- Findings and discussions (cont'd 1)
- The analysis of the results by the hierarchical analysis process method is done with the objective of **optimizing** the **solubilization** of copper, while choosing the best criteria and sub-criteria in relation to the higher hierarchical level.
- Examination of the sub-criteria shows us that optimal solubilization of copper is obtained at :
  - **Time = 2 h; Solid percentage = 20 % ;**
  - **Stirring speed = 600 rpm; Acidity = 80 g/L ;**
  - **Fe<sup>2+</sup> ion = 2 g/L**

# Co-Cu ore dissolution optimized by means of MCDA

- Findings and discussions (cont'd 2)
- Pairwise comparison of criteria, Comparison judgment matrix, Priority, Eigenvalue  $\lambda_{\max}$ , Random Index (RI), Consistency index (CI), Consistency ratio (CR).

*Table 2: Complete comparison of criteria for copper solubilization*

Comparison of criteria	% Solid	H <sub>2</sub> SO <sub>4</sub>	Time	Agitation	Fe <sup>2+</sup>	Priority
% Solid	1	2	7	8	9	0.49
H <sub>2</sub> SO <sub>4</sub>	1/2	1	5	7	8	0.33
Time	1/7	1/5	1	2	3	0.09
Stirring rate	1/8	1/7	1/2	1	2	0.06
Fe <sup>2+</sup>	1/9	1/8	1/3	1/2	1	0.04
$\lambda_{\max} = 5.12$	CI = 0.03122				CR = 2.78 %	



# Co-Cu ore dissolution optimized by means of MCDA

## • Conclusions

- It has been demonstrated how this approach assists in making **rational decisions** regarding the **optimization** of the leaching process for a composite of Cu-Co ores.
- It is therefore possible to **improve the dissolution** of a process by **synergistic association of optimization methods** well established in hydrometallurgy such as the Taguchi method.

*The End*

THANK YOU FOR YOUR ATTENTION.